

Algebra 2

1-07 Use Inverse Matrices to Solve Linear Systems (12.4)

Identity Matrix

The Identity Matrix _____ with any matrix of the _____ dimension equals the _____ matrix.

$$A \cdot I = I \cdot A = \underline{\hspace{2cm}}$$

This is the matrix equivalent of 1

$$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \quad \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

You cannot _____ by a matrix!

So we _____ by the _____ of a matrix.

$$A \cdot A^{-1} = \underline{\hspace{2cm}}$$

If A , B , and X are matrices, and

$$A \cdot X = B$$

$$A^{-1} \cdot A \cdot X = A^{-1} \cdot B$$

$$I \cdot X = A^{-1} \cdot B$$

$$X = \underline{\hspace{2cm}}$$

Inverse Matrix

The Rule for 2×2

$$\text{If } A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}, \text{ then } A^{-1} = \frac{1}{\begin{vmatrix} a & b \\ c & d \end{vmatrix}} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}^{-1}$$

$$\begin{bmatrix} -2 & -1 \\ 4 & 0 \end{bmatrix}^{-1}$$

Solve a matrix equation

$$AX = B$$

$$\begin{bmatrix} -3 & 4 \\ 5 & -7 \end{bmatrix} X = \begin{bmatrix} 3 & 8 \\ 2 & -2 \end{bmatrix}$$

Solve a system of linear equations

$$2x + y = -13$$

$$x - 3y = 11$$